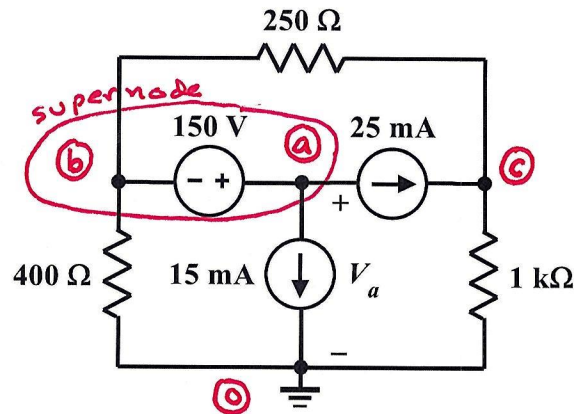


EE 2240
Homework Problem #024

Use the nodal analysis method to determine V_a .



$$V_a - V_b = 150 \text{ V} \quad (\text{constraint equation for supernode})$$

$$\frac{V_b - V_c}{250 \Omega} + 25 \text{ mA} + 15 \text{ mA} + \frac{V_b}{400 \Omega} \quad (\text{KCL for supernode})$$

$$\frac{V_c - V_b}{250 \Omega} - 25 \text{ mA} + \frac{V_c}{1 \text{ k}\Omega} = 0 \quad (\text{KCL for node c})$$

In matrix form:

$$\begin{bmatrix} 1 & -1 & 0 \\ 0 & \frac{1}{250} + \frac{1}{400} & -\frac{1}{250} \\ 0 & -\frac{1}{250} & \frac{1}{250} + \frac{1}{1000} \end{bmatrix} \begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} 150 \\ -25 \times 10^{-3} - 15 \times 10^{-3} \\ 25 \times 10^{-3} \end{bmatrix}$$

Solving yields $V_a = 143.9394 \text{ V}$

(see next page for
 MATLAB solution)

```
>> a=[1 -1 0; 0 1/250+1/400 -1/250; 0 -1/250 1/250+1/1000]
```

```
a =
```

```
1.0000 -1.0000 0  
0 0.0065 -0.0040  
0 -0.0040 0.0050
```

```
>> c=[150 -25e-3-15e-3 25e-3]'
```

```
c =
```

```
150.0000  
-0.0400  
0.0250
```

```
>> b=a\c
```

```
b =
```

```
143.9394  
-6.0606  
0.1515
```